



Hochschule
München
University of
Applied Sciences

Laboratory for
Mechatronic
and Renewable
Energy Systems
(LMRES)

A generic framework to minimize copper and iron losses in electrical machines in real time

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Outline

- Introduction
- 1 Motivation
- 2 Problem statement and proposed solution
- 3 Optimal operation strategies and operation management
- 4 Implementation results
- 5 Conclusion

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Introduction

LMRES (lmres.ee.hm.edu) - International team and collaborations



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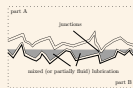
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Introduction

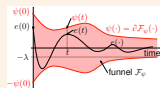
LMRES – Interdisciplinary expertise und publications (> 140 peer-reviewed publications)



System identification
[9–14]



Friction
[15, 16]



Control & Systems Theory
[15, 17–32]



Paper coating machines
[4–8]



Didactics/Teaching
[32, 136–144]



Robotics & Mechatronics
[15, 16, 32–43]



Electro-active polymers
[1–3]

Mechatronics & renewable energy systems



Power electronics
[32, 44–80]



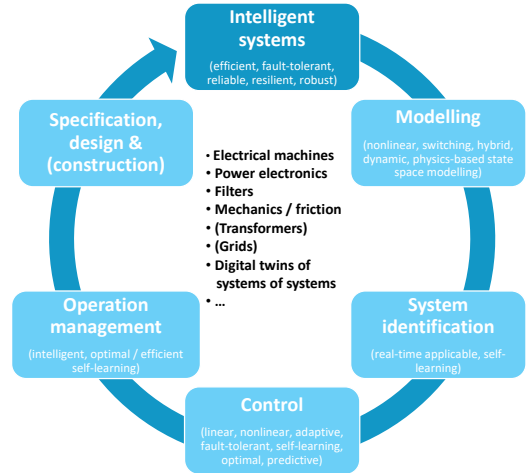
Renewable energy systems [13, 29, 31, 32, 45, 46, 52, 53, 55–57, 59, 61, 67, 72, 73, 78–80, 85–87, 90, 92, 99, 104, 113–135]



Electrical drives (motors/generators)
[13, 15, 17, 19, 20, 30, 32, 38, 42, 54, 62, 67, 69, 72, 81–112]

Introduction

LMRES – Research projects and research goals (funding: > 4.3 million €; e.g. DAAD, Bavaria, BMBF, BMWi, DFG, EU)



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Motivation

Electrical machines: Widely-used, compact and efficient actuators



www.farmwood.co.uk



www.abb.com (from video)



www.bmw.de



www.siemens.com



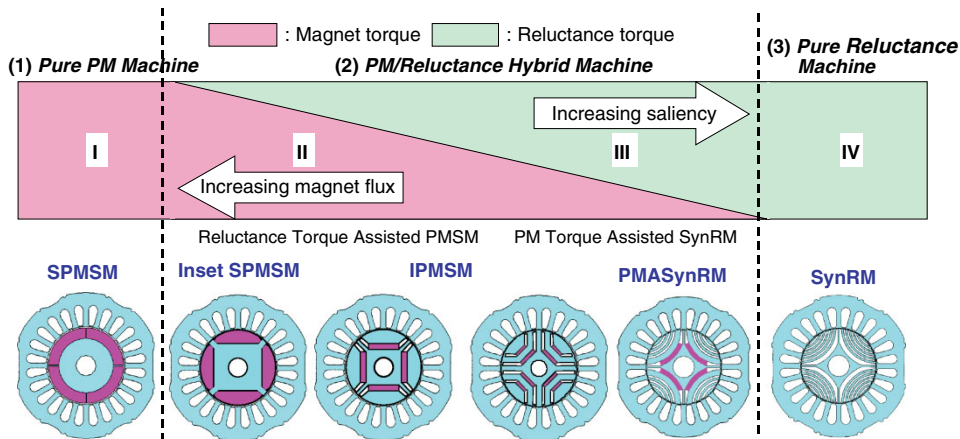
www.lilium.com

...

- buildings (e.g. air conditioning or fans)
- industrial applications (e.g. pumps)
- traction drives (e.g. electric vehicles, trains, etc.)
- power generation (e.g. conventional power plants or wind turbine systems)
- (more) electric aircrafts

Motivation

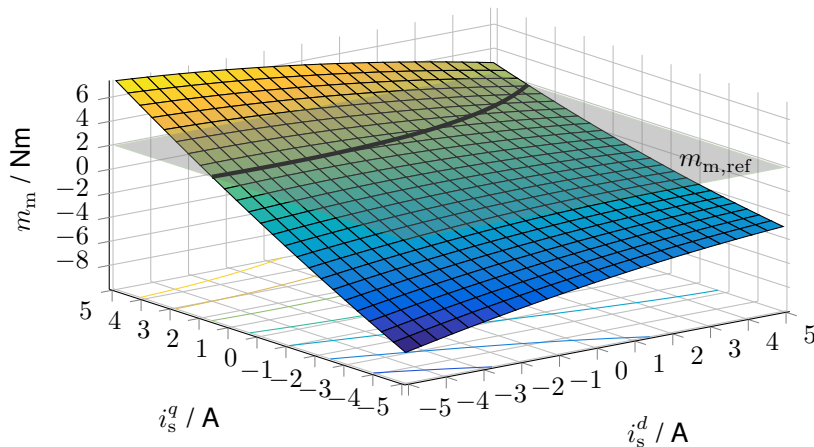
Examples of anisotropic synchronous machines [145] with “saliency ratio” $L_s^d/L_s^q \neq 1$



$$m_m(i_s^d, i_s^q) = \frac{2n_p}{3\kappa^2} (i_s^{dq})^\top \mathbf{J} \psi_s^{dq} \stackrel{\text{(const. Para.)}}{=} \frac{2n_p}{3\kappa^2} \left[\underbrace{\tilde{\psi}_{pm} i_s^q}_{\text{magnetic torque}} + \underbrace{(\tilde{L}_s^d - \tilde{L}_s^q) i_s^d i_s^q}_{\text{reluctance torque}} + \underbrace{\tilde{L}_{s,m} ((i_s^q)^2 - (i_s^d)^2)}_{\text{cross-coupling torque}} \right]$$

Motivation

Optimal feedforward torque control problem: **Anisotropic, affine PMSM** (without iron losses)

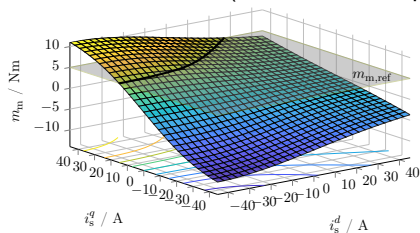


$$m_{m,\text{ref}} \stackrel{!}{=} m_m(i_s^{dq}) = \frac{2n_p}{3\kappa^2} \left[\tilde{\psi}_{\text{pm}} i_s^q + (\tilde{L}_s^d - \tilde{L}_s^q) i_s^d i_s^q + \tilde{L}_{s,m} ((i_s^q)^2 - (i_s^d)^2) \right] \implies \boxed{i_{s,\text{ref}}^{dq} := (\textcolor{red}{?}, \textcolor{red}{?})^\top}$$

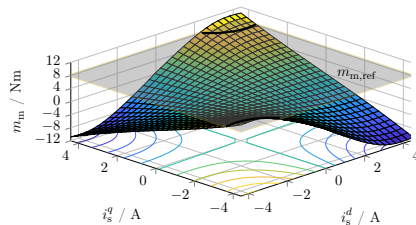
Motivation

Optimal feedforward torque control problem: **Identical for all (nonlinear) machines**

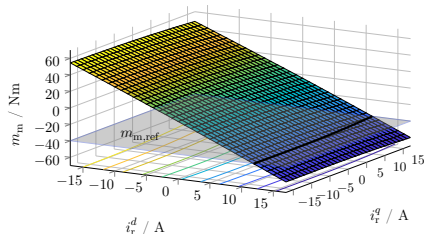
Nonlinear IPMSM (3.9 kW@5 500 rpm)



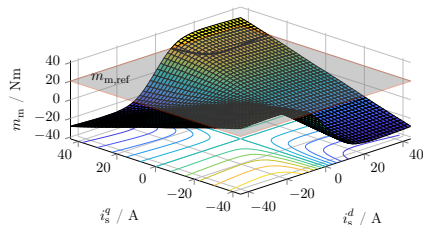
Nonlinear IM (3 kW@1 445 rpm)



Nonlinear DFIM (10 kW@1 500 rpm)



Nonlinear RSM (9.6 kW@1 500 rpm)

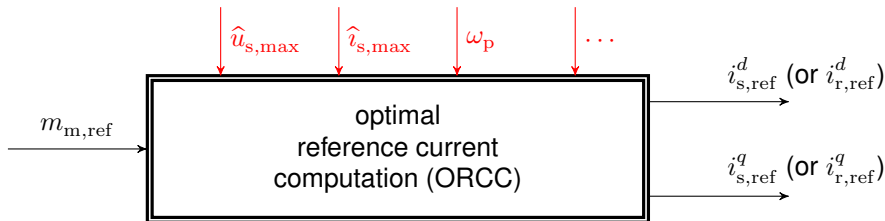


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Problem statement and proposed solution

Optimal feedforward torque control problem: Optimal reference current computation (ORCC)



$$\mathbf{i}_{s,ref}^{dq}(m_{m,ref}, \hat{u}_{s,max}, \hat{i}_{s,max}, \omega_p, \dots) = \begin{pmatrix} i_{s,ref}^d(m_{m,ref}, \hat{u}_{s,max}, \hat{i}_{s,max}, \omega_p, \dots) \\ i_{s,ref}^q(m_{m,ref}, \hat{u}_{s,max}, \hat{i}_{s,max}, \omega_p, \dots) \end{pmatrix}$$

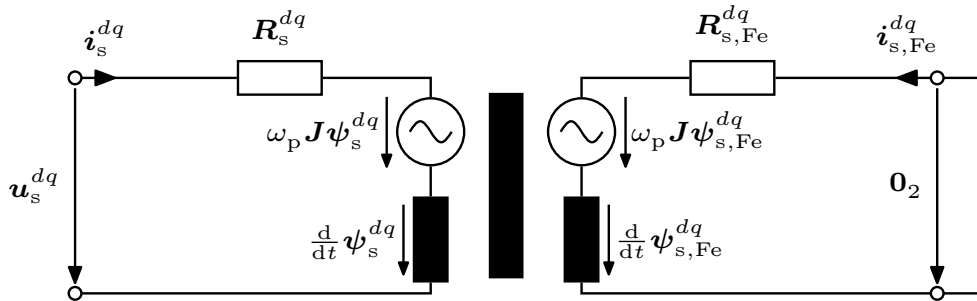
(✓) Numerical solutions and/or look-up tables
(but: limited storage, accuracy, real-time applicability)

? Analytical solutions

(some do exist but impose simplifying assumptions such as $R_s = 0$, $R_{s,Fe} = 0$ and/or $L_{s,m} = 0$, etc.)

Problem statement and proposed solution

Considered anisotropic synchronous machines with iron losses: **Nonlinear transformer model**



with $\psi_s^{dq} = \psi_{s,Fe}^{dq}$ (single assumption!) and (possibly) *nonlinear*

- *current, angle, speed and temperature dependent stator resistance, i.e.* $R_s^{dq} := R_s^{dq}(i_s^{dq}, \phi_p, \omega_p, \vartheta_s)$
- *current, angle, speed and temperature dependent iron resistance, i.e.* $R_{s,Fe}^{dq} := R_{s,Fe}^{dq}(i_s^{dq}, \phi_p, \omega_p, \vartheta_s)$
- *current, angle, speed and temperature dependent flux linkages, i.e.* $\psi_s^{dq} := \psi_s^{dq}(i_s^{dq}, \phi_p, \omega_p, \vartheta_s)$

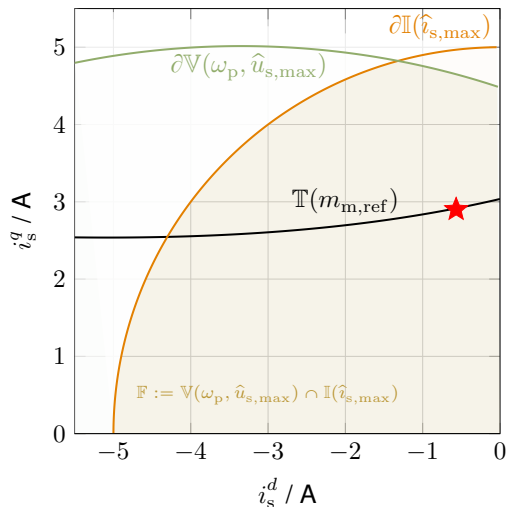
Problem statement and proposed solution

Considered anisotropic synchronous machines with iron losses: **Nonlinear machine dynamics** ($\implies$ steady-state model)

$$\begin{aligned}
 \text{Stator:} \quad & \underbrace{\begin{pmatrix} u_s^d \\ u_s^q \end{pmatrix}}_{=: \mathbf{u}_s^{dq}} = \underbrace{\begin{bmatrix} R_s^d & R_s^{dq} \\ R_s^{qd} & R_s^q \end{bmatrix}}_{=: \mathbf{R}_s^{dq}} \underbrace{\begin{pmatrix} i_s^d \\ i_s^q \end{pmatrix}}_{=: \mathbf{i}_s^{dq}} + \omega_p \underbrace{\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}}_{=: \mathbf{J}} \underbrace{\begin{pmatrix} \psi_s^d \\ \psi_s^q \end{pmatrix}}_{=: \mathbf{\psi}_s^{dq}} + \cancel{\frac{d}{dt} \psi_s^{dq}} \\
 \text{Iron:} \quad & \underbrace{\begin{pmatrix} 0 \\ 0 \end{pmatrix}}_{=: \mathbf{0}_2} = \underbrace{\begin{bmatrix} R_{s,Fe}^d & R_{s,Fe}^{dq} \\ R_{s,Fe}^{qd} & R_{s,Fe}^q \end{bmatrix}}_{=: \mathbf{R}_{s,Fe}^{dq}} \underbrace{\begin{pmatrix} i_{s,Fe}^d \\ i_{s,Fe}^q \end{pmatrix}}_{=: \mathbf{i}_{s,Fe}^{dq}} + \omega_p \mathbf{J} \mathbf{\psi}_s^{dq} + \cancel{\frac{d}{dt} \psi_s^{dq}} \\
 & \mathbf{i}_{s,Fe}^{dq} = -(\mathbf{R}_{s,Fe}^{dq})^{-1} \left[\omega_p \mathbf{J} \mathbf{\psi}_s^{dq} + \cancel{\frac{d}{dt} \psi_s^{dq}} \right] \\
 \text{Mech.:} \quad & \frac{d}{dt} \omega_m = \frac{1}{\Theta_m} (m_m + m_l) \quad \text{with} \quad \omega_p = n_p \omega_m \\
 & m_m = \frac{2}{3\kappa^2} (\mathbf{i}_s^{dq} + \mathbf{i}_{s,Fe}^{dq})^\top \mathbf{J} \mathbf{\psi}_s^{dq} \\
 \text{Losses:} \quad & p_{s,L} = \underbrace{\frac{2}{3\kappa^2} (\mathbf{i}_s^{dq})^\top \mathbf{R}_s^{dq} \mathbf{i}_s^{dq}}_{=: p_{s,Cu}} + \underbrace{\frac{2}{3\kappa^2} (\mathbf{i}_{s,Fe}^{dq})^\top \mathbf{R}_{s,Fe}^{dq} \mathbf{i}_{s,Fe}^{dq}}_{=: p_{s,Fe}}
 \end{aligned}$$

Problem statement and proposed solution

Optimal reference current computation (ORCC): Optimization problem(s) with multiple constraints



$$\max_{\mathbf{i}_s^{dq} \in \mathbb{F}} -f(\mathbf{i}_s^{dq}) \quad \text{subject to}$$

$$\left\{ \begin{array}{l} \|\mathbf{i}_s^{dq}\|^2 \leq \hat{i}_{s,max}^2, \\ \text{(current circular area)} \\ \|\mathbf{u}_s^{dq}(\mathbf{i}_s^{dq}, \omega_p, \dots)\|^2 \leq \hat{u}_{s,max}^2, \\ \text{(voltage elliptical area)} \\ |m_m(\mathbf{i}_s^{dq}, \omega_p, \dots)| \leq |m_{m,ref}|, \\ \text{and } \text{sign}(m_{m,ref}) = \\ \text{sign}(m_m(\mathbf{i}_s^{dq})). \end{array} \right.$$

$\Rightarrow$ e.g. minimize copper losses,
i.e., $-f(\mathbf{i}_s^{dq}) = -\|\mathbf{i}_s^{dq}\|^2$.

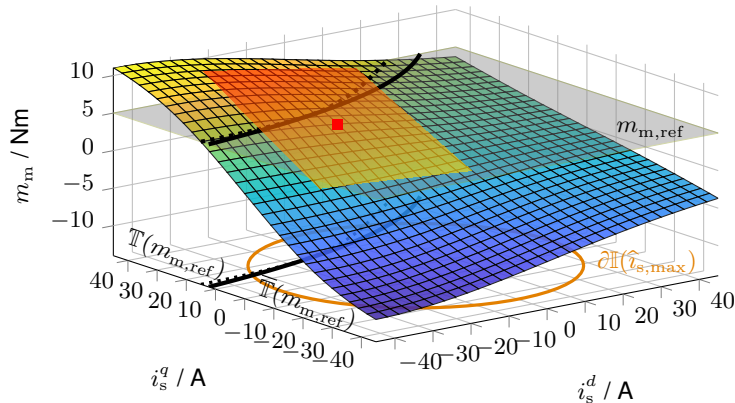
$\Rightarrow \mathbf{i}_{s,ref}^{dq} = \mathbf{i}_{s,MTPC}^{dq}$ at ★, i.e., MTPC
with $m_{m,ref} = m_m(\mathbf{i}_{s,ref}^{dq})$ feasible.

Problem statement and proposed solution

Proposed solution: **Online linearization, implicit formulation (quadratics), optimization and intersection points**

Step 1: Online linearization of flux linkages, machine torque, iron resistance, etc.: for example:

- **flux linkages** (first-order Taylor approximation around operating point $\bar{i}_s^{dq}$ [■])
- **machine torque** (second-order Taylor approximation around operating point $\bar{i}_s^{dq}$ [■])



Problem statement and proposed solution

Proposed solution: **Online linearization, implicit formulation (quadrics), optimization and intersection points**

Step 2: Derivation of quadrics $Q_A(\mathbf{i}_s^{dq}) := (\mathbf{i}_s^{dq})^\top \mathbf{A} \mathbf{i}_s^{dq} + 2\mathbf{a}^\top \mathbf{i}_s^{dq} + \alpha$:

- Current circular area: $(i_s^d)^2 + (i_s^q)^2 \leq \hat{i}_{s,\max}^2 \iff \|\mathbf{i}_s^{dq}\|^2 = (\mathbf{i}_s^{dq})^\top \mathbf{I}_2 \mathbf{i}_s^{dq} \leq \hat{i}_{s,\max}^2$

$$\implies \mathbb{I}(\hat{i}_{s,\max}) := \{ \mathbf{i}_s^{dq} \in \mathbb{R}^2 \mid (\mathbf{i}_s^{dq})^\top \mathbf{I}_2 \mathbf{i}_s^{dq} - \hat{i}_{s,\max}^2 \leq 0 \}$$

- (Linearized) Voltage elliptical area: $(u_s^d)^2 + (u_s^q)^2 \leq \hat{u}_{s,\max}^2 \iff \|\mathbf{u}_s^{dq}(\mathbf{i}_s^{dq}, \omega_p, \dots)\|^2 = \dots \leq \hat{u}_{s,\max}^2$

$$\implies \overline{\mathbb{V}}(\hat{u}_{s,\max}) := \{ \mathbf{i}_s^{dq} \in \mathbb{R}^2 \mid (\mathbf{i}_s^{dq})^\top \overline{\mathbf{V}}(\bar{\omega}_p) \mathbf{i}_s^{dq} + 2\bar{\mathbf{v}}(\bar{\omega}_p)^\top \mathbf{i}_s^{dq} + \bar{\nu}(\bar{\omega}_p, \hat{u}_{s,\max}) \leq 0 \}$$

- (Linearized) Reference torque hyperbola: $m_m(\mathbf{i}_s^{dq}, \omega_p, \dots) = \frac{3}{2}n_p(\mathbf{i}_s^{dq} + \mathbf{i}_{s,\text{Fe}}^{dq})^\top \mathbf{J}\boldsymbol{\psi}_s^{dq} \stackrel{!}{=} m_{m,\text{ref}} \iff \dots$

$$\implies \overline{\mathbb{T}}(m_{m,\text{ref}}) := \{ \mathbf{i}_s^{dq} \in \mathbb{R}^2 \mid (\mathbf{i}_s^{dq})^\top \overline{\mathbf{T}} \mathbf{i}_s^{dq} + 2\bar{\mathbf{t}}^\top \mathbf{i}_s^{dq} - m_{m,\text{ref}} = 0 \}$$

■ ...

Problem statement and proposed solution

Proposed solution: **Online linearization, implicit formulation (quadrics), optimization and intersection points**

Step 3: Optimization problem with equality constraint

$$\max_{\mathbf{i}_s^{dq}} - \left(\underbrace{(\mathbf{i}_s^{dq})^\top \mathbf{A} \mathbf{i}_s^{dq} + 2\mathbf{a}^\top \mathbf{i}_s^{dq} + \alpha}_{=: Q_A(\mathbf{i}_s^{dq})} \right) \text{ s.t. } \underbrace{(\mathbf{i}_s^{dq})^\top \mathbf{B} \mathbf{i}_s^{dq} + 2\mathbf{b}^\top \mathbf{i}_s^{dq} + \beta}_{=: Q_B(\mathbf{i}_s^{dq})} = 0$$

$\implies$ Hyperbolas for e.g. MTPC, MTPL or MTPV (with $R_s, R_{s,Fe} \neq 0$ & $L_{s,m} \neq 0$, etc.)

Step 4: Intersection of two quadrics (e.g. voltage ellipse and current circle)

$$\mathbf{i}_{s,\text{ref}}^{dq} := \arg \min_{\|\mathbf{i}_s^{dq}\|} \left\{ \mathbf{i}_s^{dq} \in \mathbb{R}^2 \mid Q_A(\mathbf{i}_s^{dq}) = 0 \wedge Q_B(\mathbf{i}_s^{dq}) = 0 \right\}$$

$\implies$ Optimal operation point ★ (reference current; iteration possibly necessary)

Both lead to subproblem of solving a fourth-order (quartic) polynomial

$$\chi(\lambda) := c_4 \lambda^4 + c_3 \lambda^3 + c_2 \lambda^2 + c_1 \lambda + c_0 \stackrel{!}{=} 0$$

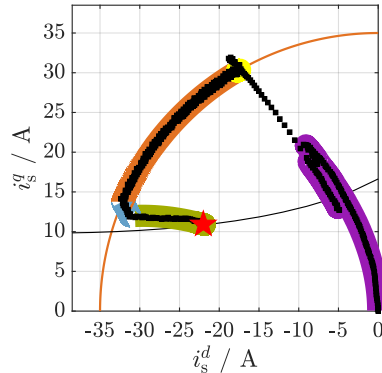
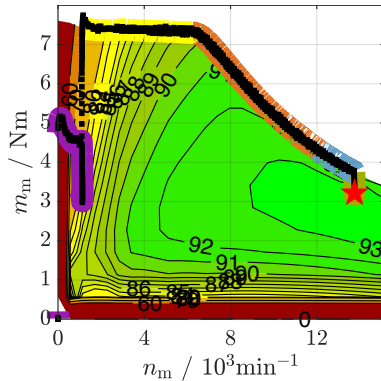
$\implies$ Analytical solutions exist (e.g. Euler's solution, see [146])

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Optimal operation strategies and operation management

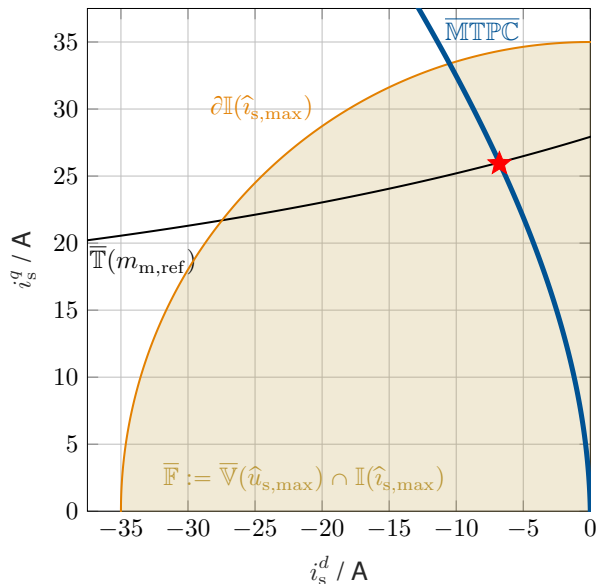
Overview of operation strategies



- Maximum Torque per Losses (MTPL) [purple] (or Maximum Torque per Current (MTPC) [blue])
- Maximum Current (MC) [orange] (and Maximum Current extended (MC_{ext}) [yellow])
- Maximum Torque per Voltage (MTPV) [light blue] (or Maximum Torque per Flux (MTPF))
- Field Weakening (FW) [light green]

Optimal operation strategies and operation management

Maximum Torque per Current (**MTPC** @ $0 \cdot \omega_{m,R}$): Reference torque **feasible**



Optimization problem

$$\begin{aligned} \max_{\mathbf{i}_s^{dq} \in \bar{\mathbb{F}}} -p_{s,Cu}(\mathbf{i}_s^{dq}) \quad \text{s.t.} \\ \underbrace{(\mathbf{i}_s^{dq})^\top \bar{\mathbf{T}} \mathbf{i}_s^{dq} + 2 \bar{\mathbf{t}}^\top \mathbf{i}_s^{dq}}_{\approx m_m(\mathbf{i}_s^{dq})} - m_{m,\text{ref}} = 0 \end{aligned}$$

Solution set

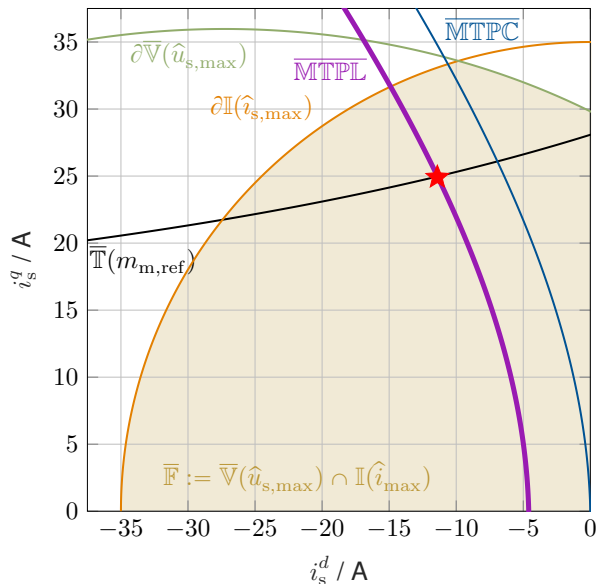
$$\begin{aligned} \overline{\text{MTPC}}(\bar{\mathbf{i}}_s^{dq}, \bar{\omega}_p, \dots) &:= \{ \mathbf{i}_s^{dq} \in \mathbb{R}^2 \mid \\ &(\mathbf{i}_s^{dq})^\top \bar{\mathbf{M}}_C \mathbf{i}_s^{dq} + 2 \bar{\mathbf{m}}_C^\top \mathbf{i}_s^{dq} = 0 \} \end{aligned}$$

Optimal reference currents (★)

$$\mathbf{i}_{s,\text{MTPC}}^{dq} = \overline{\text{MTPC}} \cap \bar{\mathbf{T}}(m_{m,\text{ref}})$$

Optimal operation strategies and operation management

Maximum Torque per Losses (**MTPL** @ $1 \cdot \omega_{m,R}$): Reference torque **feasible**



Optimization problem

$$\begin{aligned} \max_{\mathbf{i}_s^{dq} \in \bar{\mathbb{F}}} & -p_{s,Cu}(\mathbf{i}_s^{dq}) - p_{s,Fe}(\mathbf{i}_s^{dq}) \quad \text{s.t.} \\ & \underbrace{(\mathbf{i}_s^{dq})^\top \bar{\mathbf{T}} \mathbf{i}_s^{dq} + 2 \bar{\mathbf{t}}^\top \mathbf{i}_s^{dq}}_{\approx m_m(\mathbf{i}_s^{dq})} - m_{m,ref} = 0 \end{aligned}$$

Solution set

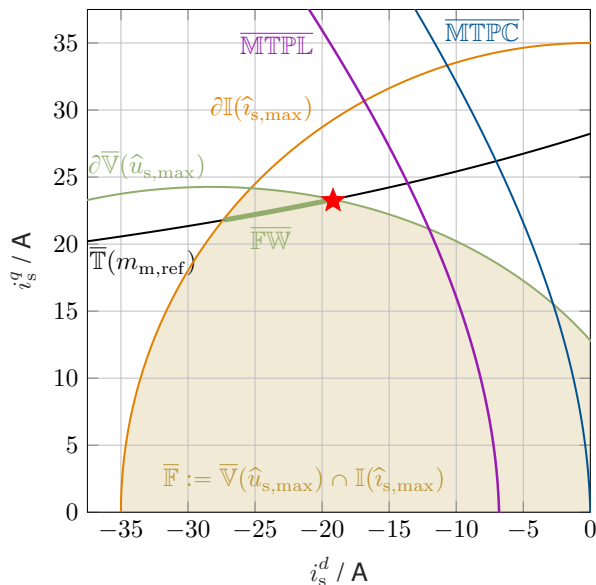
$$\begin{aligned} \overline{\text{MTPL}}(\bar{\mathbf{i}}_s^{dq}, \bar{\omega}_p, \dots) &:= \{ \mathbf{i}_s^{dq} \in \mathbb{R}^2 \mid \\ & (\mathbf{i}_s^{dq})^\top \bar{\mathbf{M}}_L \mathbf{i}_s^{dq} + 2 \bar{\mathbf{m}}_L^\top \mathbf{i}_s^{dq} + \bar{\mu}_L = 0 \} \end{aligned}$$

Optimal reference currents (★)

$$\mathbf{i}_{s,MTPL}^{dq} = \overline{\text{MTPL}} \cap \bar{\mathbf{T}}(m_{m,ref})$$

Optimal operation strategies and operation management

Field Weakening (**FW** @ $1.40 \cdot \omega_{m,R}$): Reference torque **feasible**



Optimization problem

$$\begin{aligned} \max_{\mathbf{i}_s^{dq} \in \bar{\mathbb{F}}} & -p_{s,Cu}(\mathbf{i}_s^{dq}) - p_{s,Fe}(\mathbf{i}_s^{dq}) \quad \text{s.t.} \\ & \underbrace{(\mathbf{i}_s^{dq})^\top \mathbf{T} \mathbf{i}_s^{dq} + 2 \mathbf{t}^\top \mathbf{i}_s^{dq}}_{=m_m(\mathbf{i}_s^{dq})} - m_{m,ref} = 0 \end{aligned}$$

Feasible set

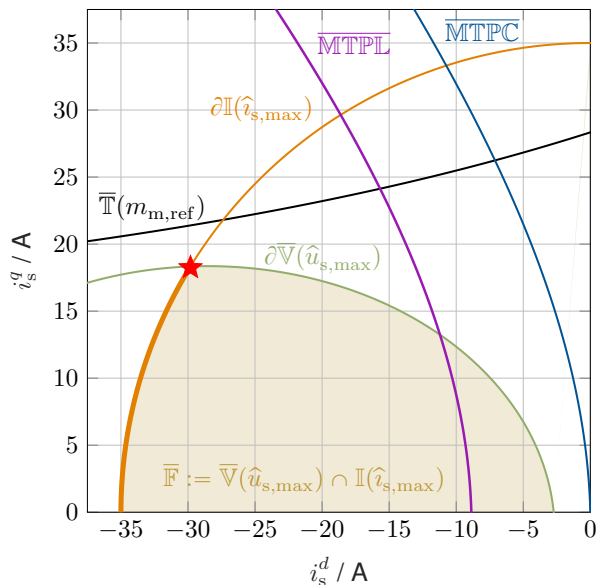
$$\begin{aligned} \bar{\mathbb{F}}\bar{\mathbb{W}}(\bar{\mathbf{i}}_s^{dq}, \bar{\omega}_p, \dots, m_{m,ref}, \hat{u}_{s,max}, \hat{i}_{s,max}) := \\ \bar{\mathbb{F}}(\hat{u}_{s,max}, \hat{i}_{s,max}) \cap \bar{\mathbb{T}}(m_{m,ref}) \end{aligned}$$

Optimal reference currents (★)

$$\mathbf{i}_{s,FW}^{dq} = \partial \bar{\mathbb{V}}(\hat{u}_{s,max}) \cap \bar{\mathbb{T}}(m_{m,ref})$$

Optimal operation strategies and operation management

Maximum Current (**MC** @ $2 \cdot \omega_{m,R}$): Reference torque **not feasible**



Optimization problem

$$\max_{\substack{i_s^{dq} \in \bar{\mathbb{F}}}} |(m_m(i_s^{dq}))| \quad \text{s.t.} \\ \text{sign}(m_m) = \text{sign}(m_{m,\text{ref}})$$

Feasible set

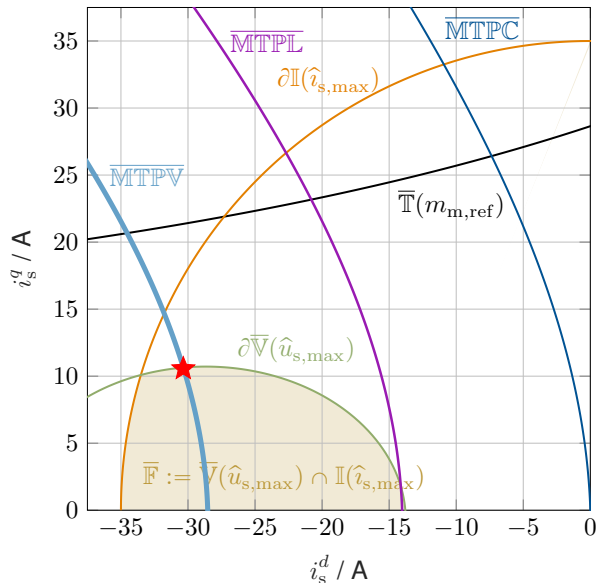
$$\overline{\text{MC}}(\bar{i}_s^{dq}, \bar{\omega}_p, \dots, \hat{u}_{s,\text{max}}, \hat{i}_{s,\text{max}}) := \bar{\mathbb{V}}(\hat{u}_{s,\text{max}}) \cap \partial \mathbb{I}(\hat{i}_{s,\text{max}})$$

Optimal current reference (★)

$$i_{s,\text{MC}}^{dq} = \partial \bar{\mathbb{V}}(\hat{u}_{s,\text{max}}) \cap \partial \mathbb{I}(\hat{i}_{s,\text{max}})$$

Optimal operation strategies and operation management

Maximum Torque per Voltage (**MTPV** @ $3.50 \cdot \omega_{m,R}$): Reference torque **not feasible**



Optimization problem

$$\begin{aligned} \max_{\mathbf{i}_s^{dq} \in \bar{\mathbf{F}}} & -\|\mathbf{u}_s^{dq}(\mathbf{i}_s^{dq})\|^2 \quad \text{s.t.} \\ & \underbrace{(\mathbf{i}_s^{dq})^\top \bar{\mathbf{T}} \mathbf{i}_s^{dq} + 2 \bar{\mathbf{t}}^\top \mathbf{i}_s^{dq}}_{=m_m(\mathbf{i}_s^{dq})} - m_{m,\text{ref}} = 0 \end{aligned}$$

Solution set

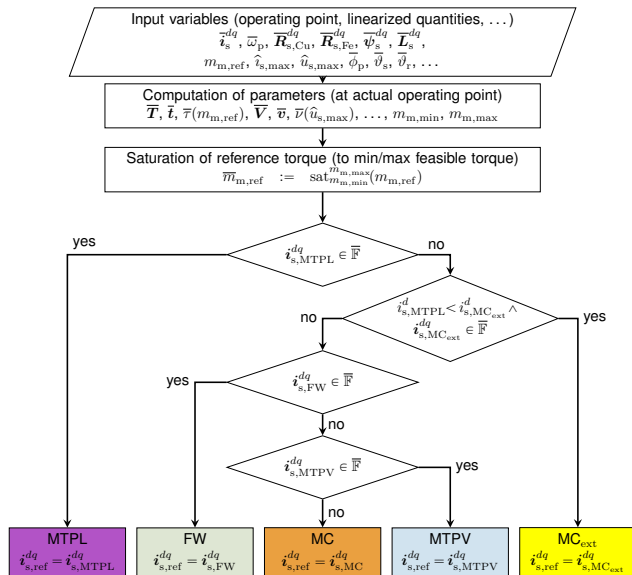
$$\overline{\text{MTPV}}(\bar{\mathbf{i}}_s^{dq}, \bar{\omega}_p, \dots) := \left\{ \mathbf{i}_s^{dq} \in \mathbb{R}^2 \mid (\mathbf{i}_s^{dq})^\top \bar{\mathbf{M}}_V \mathbf{i}_s^{dq} + 2 \bar{\mathbf{m}}_V^\top \mathbf{i}_s^{dq} + \bar{\mu}_V = 0 \right\}$$

Optimal reference currents (★)

$$\mathbf{i}_{s,\text{MTPV}}^{dq} = \overline{\text{MTPV}} \cap \partial \bar{\mathbf{V}}(\hat{\mathbf{u}}_{s,\text{max}})$$

Optimal operation strategies and operation management

Operation management and decision tree



Outline

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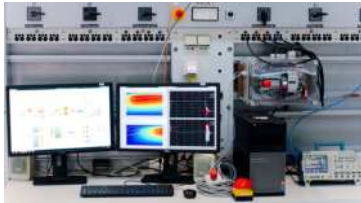
Implementation results

Exemplary laboratory setup

Reluctance SM (RSM) and Permanent-magnet SM



Host PC (rapid prototyping)

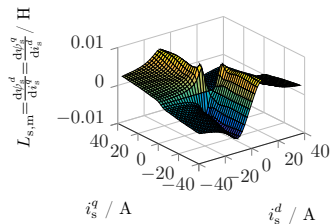
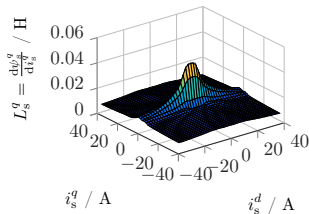
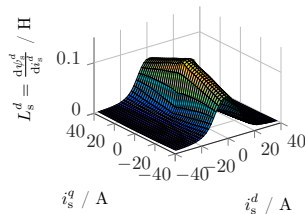
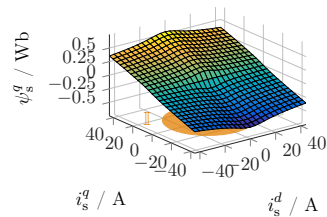
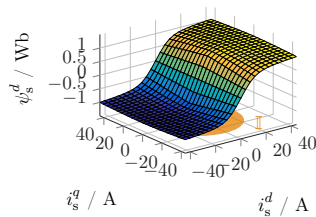
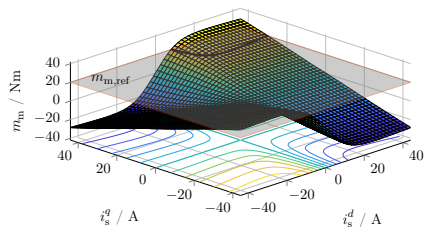


Real-time system and VSIs



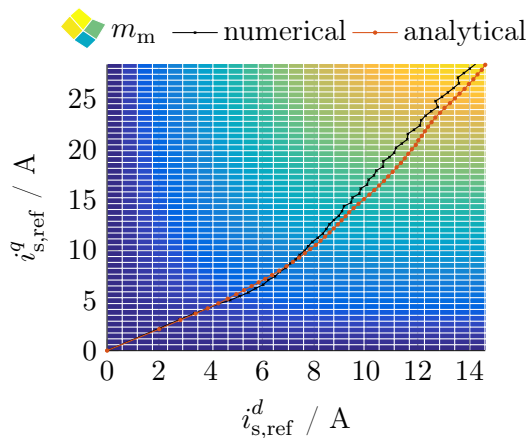
Implementation results

RSM (9.6 kW@1 500 rpm): Nonlinear maps of torque, flux linkages and differential inductances

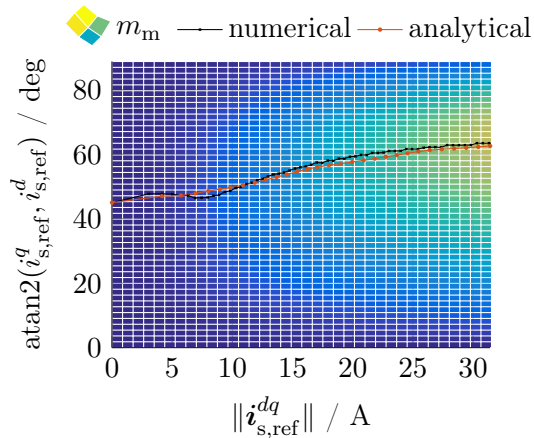


Implementation results

RSM (9.6 kW@1 500 rpm): Comparison of numerical and analytical solutions for MTPC



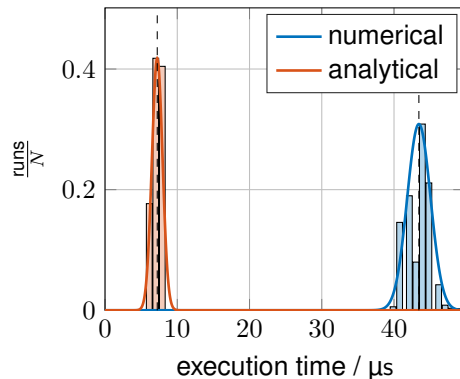
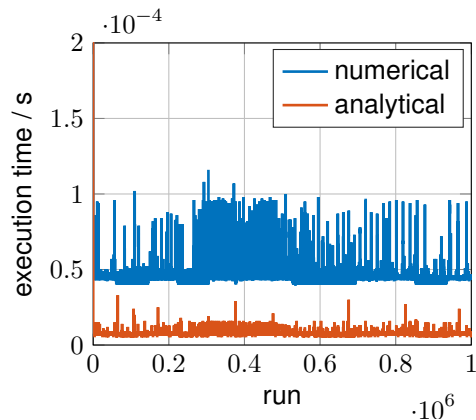
Cartesian coordinates



polar coordinates

Implementation results

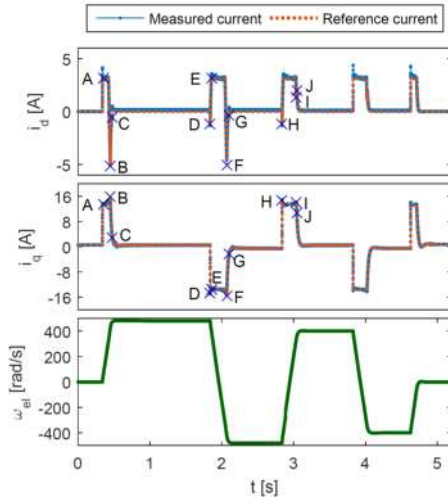
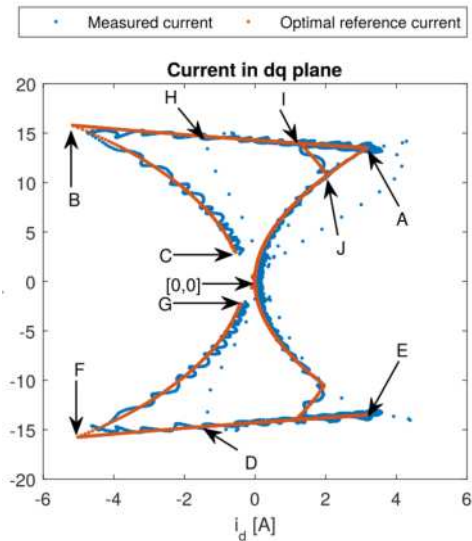
RSM (9.6 kW@1 500 rpm): Comparison of computational load



- Execution times for $N = 10^6$ runs (downsampled by factor 100)
- Standard deviations $\sigma_n = 1.61 \cdot 10^{-6} \text{ s}$ and $\sigma_a = 0.73 \cdot 10^{-6} \text{ s}$
- Average execution times $\mu_n = 43.4 \cdot 10^{-6} \text{ s}$ and $\mu_a = 7.23 \cdot 10^{-6} \text{ s}$ (**>6x faster**)

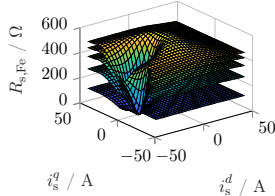
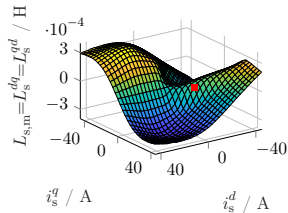
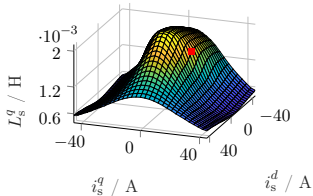
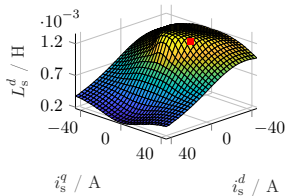
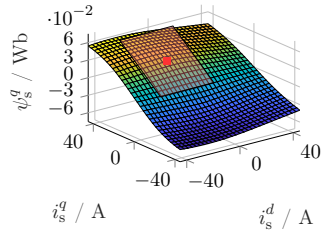
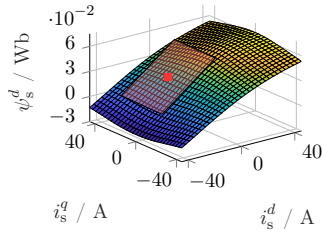
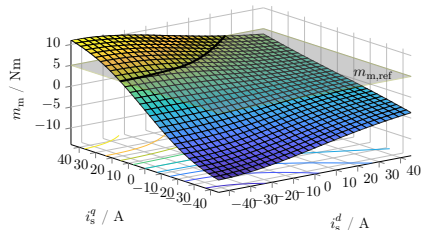
Implementation results

PME-RSM (4.5 kW@1 500 rpm): Implementation by colleagues [$\max \left(L_s^d(i_s^{dq})/L_s^q(i_s^{dq}) \right) = 1.43$] [147]



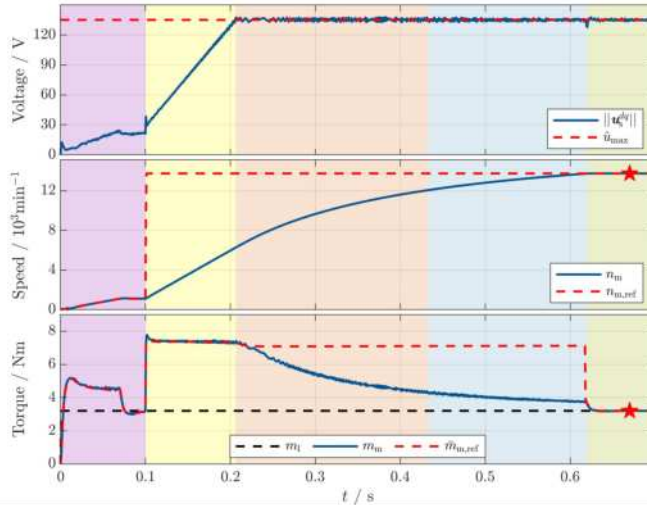
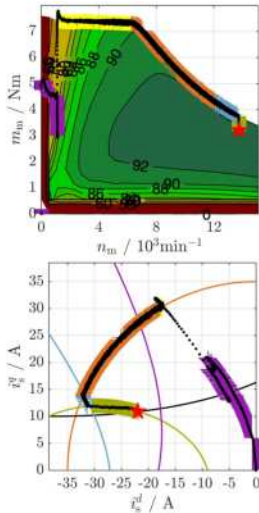
Implementation results

IPMSM (3.9 kW@5 500 rpm): Nonlinear maps of torque, flux linkages, differential inductances and iron resistance



Implementation results

IPMSM (3.9 kW@5 500 rpm): Animation



MTPL []

MC_{ext} []

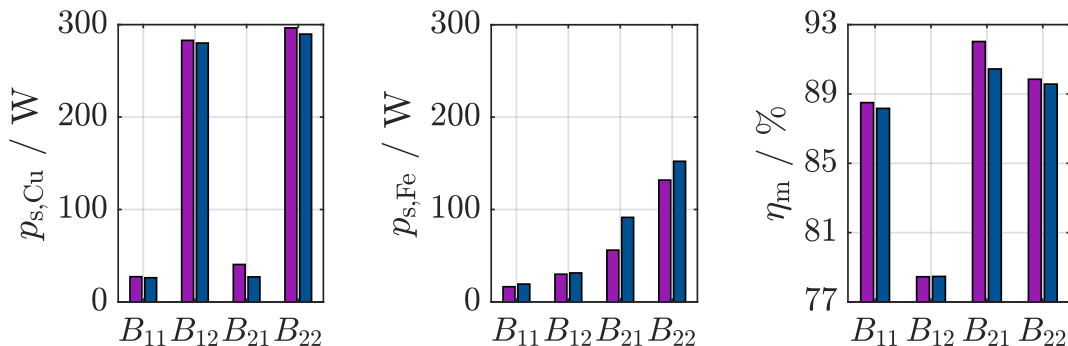
MC []

MTPV []

FW []

Implementation results

IPMSM (3.9 kW@5 500 rpm): Comparison of MTPL [■] & MTPC [■] for **four** operating points (OPs)



OP	Speed	Torque
B_{11}	30% $n_{m,R}$	30% $m_{m,R}$
B_{12}	30% $n_{m,R}$	100% $m_{m,R}$
B_{21}	100% $n_{m,R}$	30% $m_{m,R}$
B_{22}	100% $n_{m,R}$	100% $m_{m,R}$

- Copper losses increase with torque
- Iron losses increase with speed *and* torque
- MTPL outperforms MTPC for three OPs (equal for B_{12})
- highest efficiency enhancement for high speeds and low(er) torque (i.e., B_{21} with $\Delta\eta_m > 2\%$)

Outline

- Introduction
- 1 Motivation
- 2 Problem statement and proposed solution
- 3 Optimal operation strategies and operation management
- 4 Implementation results
- 5 Conclusion

Conclusion

Summary and future work

To take home

- **unified** framework for **MTPL** (MTPC), FW, $MC_{(ext)}$ & MTPV (MTPF) based on [94, 96–98, 110] and [148, Chapt. 6.9]
 - **online linearization**,
 - **quadrics** (implicit formulation),
 - **optimization problems** with **equality constraint**, and
 - **intersection** of two quadrics
- **analytical** solution for reference currents (& transition points)
- Consideration of $R_s \neq 0$, $R_{s,Fe} \neq 0$ and $L_{s,m} \neq 0$ and current, speed, angle & temperature dependency (all **simultaneously**)
- **fast(er)** and **more accurate** computation
- **applicable** in real-world (e.g. nonlinear RSM, PME-RSM or IPMSM; also IMs or DFIMs)

Future work

- convergence (mathematical proof for nonlinear flux linkages)
- more extensive experimental validation
- impact of (parameter/modelling/alignment) uncertainties
- consideration of *rotor* iron losses, *current transients* and *multi-phase* machines
- combination with minimization of *conduction and switching losses* [66]

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Journal article [97] (published 2017; doi: [10.1080/00207179.2017.1338359](https://doi.org/10.1080/00207179.2017.1338359))

INTERNATIONAL JOURNAL OF CONTROL, 2017
<https://doi.org/10.1080/00207179.2017.1338359>



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A unified theory for optimal feedforward torque control of anisotropic synchronous machines

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ABSTRACT

A unified theory for optimal feedforward torque control of anisotropic synchronous machines with *non-negligible stator resistance* and *mutual inductance* is presented which allows to *analytically* compute (1) the optimal direct and quadrature reference currents for all operating strategies, such as maximum torque per current (MTPC), maximum current, field weakening, maximum torque per voltage (MTPV) or maximum torque per flux (MTPF), and (2) the transition points indicating when to switch between the operating strategies due to speed, voltage or current constraints. The analytical solutions allow for an (almost) instantaneous selection and computation of actual operation strategy and corresponding reference currents. Numerical methods (approximating these solutions only) are *no longer* required. The unified theory is based on one simple idea: all optimisation problems, their respective constraints and the computation of the intersection point(s) of voltage ellipse, current circle or torque, MTPC, MTPV, MTPF hyperbolas are reformulated implicitly as *quadratics* which allows to invoke the Lagrangian formalism and to find the roots of fourth-order polynomials analytically. The proposed theory is suitable for any anisotropic synchronous machine. Implementation and measurement results illustrate effectiveness and applicability of the theoretical findings in real world.

ARTICLE HISTORY

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KEYWORDS

Maximum torque per ampere (MTPA); maximum torque per current (MTPC); maximum torque per voltage (MTPV); maximum torque per flux (MTPF); maximum current (MC); field weakening (FW); analytical solution; optimal feedforward torque control; efficiency; copper losses; anisotropy; synchronous machine; interior

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Conference publication (published in ICIT 2021 proceedings; not yet on IEEEExplore, see techrxiv.org)

Generic loss minimization for nonlinear synchronous machines by analytical computation of optimal reference currents considering copper and iron losses

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Abstract—The unified theory introduced in [1] allows to solve *analytically* the optimal feedforward torque control (OFTC) problem of anisotropic synchronous machines (SMs). In this paper, the theory is extended by considering relevant machine nonlinearities and incorporating copper and iron losses, thus minimizing the overall (steady-state) losses in the machine. Instead of the well known maximum torque per current (MTPC) operation strategy, *maximum torque per losses (MTPL)* is realized. The unified theory for the derivation of the analytical solution is briefly recapitulated. Moreover, current and speed dependent iron losses, as well as magnetic saturation and cross-coupling effects are considered. The resulting nonlinear optimization problem is solved via online linearization of the relevant expressions

for synchronous machines (SMs) with anisotropic rotor designs, e.g. interior permanent magnet synchronous machines (IPMSMs), reluctance synchronous machines (RSMs) or PM-assisted RMSs (PMA-RSMs), efficiency can be increased by optimal feedforward torque control (OFTC) [3, 4].

The main idea of OFTC is to exploit the ambiguity in the selection of the stator current's *direct* and *quadrature* components (producing the same amount of torque), such that losses are minimized while physical constraints are satisfied (e.g. current or voltage limits). Depending on the actual operating conditions, different optimization problems may be formulated

[A generic framework to minimize copper and iron losses in electrical machines in real time](#)

Christoph Hackl

Version from 2021/07/07

2/22

References

Conference publication (submitted to ISIE 2021; see techrxiv.org)

Optimal feedforward torque control for nonlinear induction machines considering stator & rotor copper losses and current & voltage limits

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Abstract—In order to *analytically* solve the optimal feedforward torque control (OFTC) problem of induction machines (IMs), the unified theory for synchronous machine introduced in [1] is extended by considering relevant IM *nonlinearities* and incorporating stator and rotor copper losses. Instead of the well known *Maximum Torque per (stator) Current* (MTPC) operation strategy, *Maximum Torque per (copper) Losses* (MTPL_{Cu}) is realized and extended by the *Maximum (rotor) Current* (MC_{r,ext}) strategy due to stator and rotor current limitations. Modeling magnetic saturation and cross-coupling effects leads to a constrained *nonlinear* optimization problem which is solved based on the idea of *sequential quadratic programming* (SQP). The second order Taylor approximations are formulated in implicit

generic approach can also be applied to other types of inverter-fed IMs, such as squirrel-cage induction machines (SCIMs).

The highest priority of the OFTC is to provide the reference torque while minimizing losses. In a wide operating range, there usually exist (infinitely many) different combinations of reference currents resulting in the same torque. Thus, an optimal reference current computation (ORCC) is desirable which minimizes the current-dependent IM losses while reaching the reference torque and taking into account operating (e.g. current & voltage) limits. To do so, this paper proposes a physics-based nonlinear IM model for analytical ORCC

A generic framework to minimize copper and iron losses in electrical machines in real time

Christoph Hackl

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3/22

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Chapter 6.9 in [148] (published in 2020 in Schröder “Elektrische Antriebssysteme”; doi: [10.1007/978-3-662-62700-6](https://doi.org/10.1007/978-3-662-62700-6))

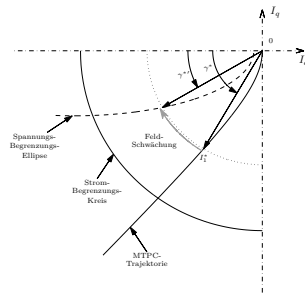
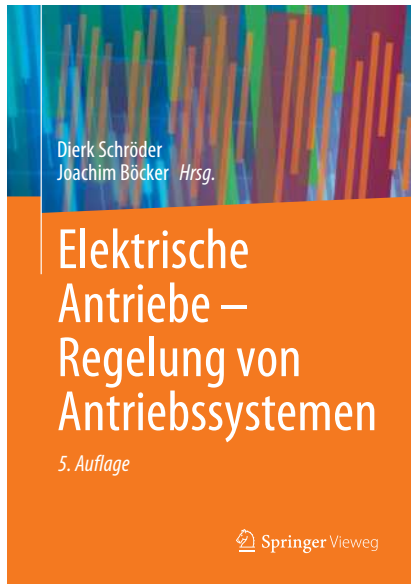


Abb. 6.101 Wirkungsweise der Feldschwächregelung mit Spannungsrückkopplung

6.9 Optimale Betriebsführung von nichtlinearen Synchronmaschinen

C. M. Hackl, J. Kullick, N. Monzen

Der folgende Abschnitt basiert auf den Publikationen [HH16; Eld+16; EHK16; Eld+17b; Hac+17; Eld+17a]. Darin wurde die erste allgemeine Theorie zur analytischen Berechnung der optimalen (verlustminimierenden) Sollströme für anisotrope Synchronmaschinen mit konstanter Erregung vorgestellt. Die weithin verbreiteten und vereinfachten Annahmen wie z. B. die Vernachlässigung des Statorwiderstandes oder der magnetischen Kreuzkopplung konnten aufgehoben werden. Zusätzlich erlaubt die Theorie die Berücksichtigung von Eisenverlusten und Nicht-

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Monograph [32] (published May 2017; doi: [10.1007/978-3-319-55036-7](https://doi.org/10.1007/978-3-319-55036-7))



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