

Current PI-funnel control with anti-windup for reluctance synchronous machines (RSMs)

Christoph Hackl

12.02.2016

Colloquium on the occasion of the 60th birthday of Achim Ilchmann

Outline

- 1 Funnel control
- 2 Current PI-funnel control with anti-windup for RSMs [1]
- 3 Conclusion

Outline

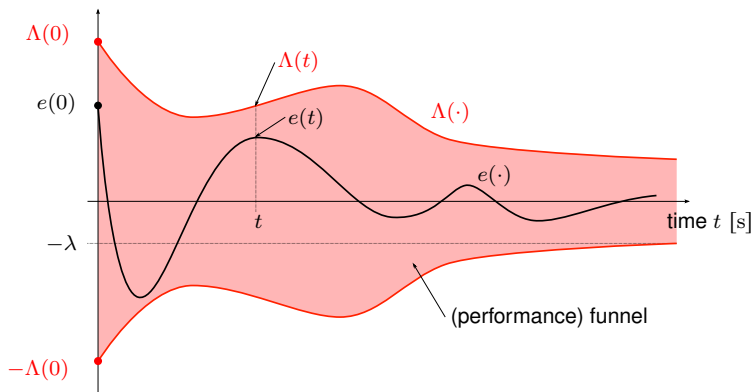
- 1** Funnel control
 - Principle idea
 - The beginning
 - Successful implementations in mechatronics

Outline

- 1 Funnel control
 - Principle idea
 - The beginning
 - Successful implementations in mechatronics

Funnel control

Tracking with prescribed transient behaviour



$$u(t) = k(t)e(t) \quad \text{with} \quad k(t) = \frac{1}{\Lambda(t) - |e(t)|}$$

Outline

1 Funnel control

- Principle idea
- The beginning
- Successful implementations in mechatronics

Funnel control

The beginning ... (at least for me in 2004)

ESAIM: Control, Optimisation and Calculus of Variations

URL: <http://www.emath.fr/cocv/>

July 2002, Vol. 7, 471–493

DOI: 10.1051/cocv:2002064

TRACKING WITH PRESCRIBED TRANSIENT BEHAVIOUR *

ACHIM ILCHMANN¹, E.P. RYAN² AND C.J. SANGWIN³

Abstract. Universal tracking control is investigated in the context of a class $\mathcal{S}$ of M -input, M -output dynamical systems modelled by functional differential equations. The class encompasses a wide variety of nonlinear and infinite-dimensional systems and contains – as a prototype subclass – all finite-dimensional linear single-input single-output minimum-phase systems with positive high-frequency gain. The control objective is to ensure that, for an arbitrary $\mathbb{R}^M$ -valued reference signal r of class $W^{1,\infty}$ (absolutely continuous and bounded with essentially bounded derivative) and every system of class $\mathcal{S}$, the tracking error e between plant output and reference signal evolves within a prespecified performance envelope or funnel in the sense that $\varphi(t)\|e(t)\| < 1$ for all $t \geq 0$, where φ a prescribed real-valued function of class $W^{1,\infty}$ with the property that $\varphi(s) > 0$ for all $s > 0$ and $\liminf_{s \rightarrow \infty} \varphi(s) > 0$. A simple (neither adaptive nor dynamic) error feedback control of the form $u(t) = -\alpha(\varphi(t)\|e(t)\|)e(t)$ is introduced which achieves the objective whilst maintaining boundedness of the control and of the scalar gain $\alpha(\varphi(\cdot)\|e(\cdot)\|)$.

Mathematics Subject Classification. 93D15, 93C30, 34K20.

Received February 7, 2002. Revised April 17, 2002.

Outline

- 1** Funnel control
 - Principle idea
 - The beginning
 - Successful implementations in mechatronics

Funnel control

Successful implementations in mechatronics (since 2004, [1–33])

Industrial drives



speed & position control

Industrial robots



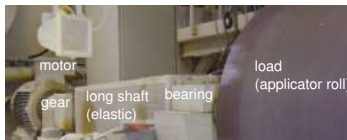
position control

Wind turbine systems



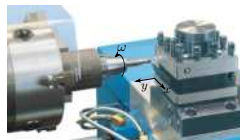
speed control

Elastic drive trains



speed & position control + damping

Machine tools



speed & position control

Electrical machines



current control

Outline

2 Current PI-funnel control with anti-windup for RSMs [1]

- Motivation and problem formulation
- Structural system properties of the RSM
- PI-funnel control with anti-windup
- Implementation and results

Outline

2 Current PI-funnel control with anti-windup for RSMs [1]

- Motivation and problem formulation
- Structural system properties of the RSM
- PI-funnel control with anti-windup
- Implementation and results

Motivation and problem formulation

Reluctance synchronous machine (RSM): A viable alternative?



Traditional IE2 induction motor



IE4 SynRM motor



<http://www.abb.com>

advantages [34–36]:

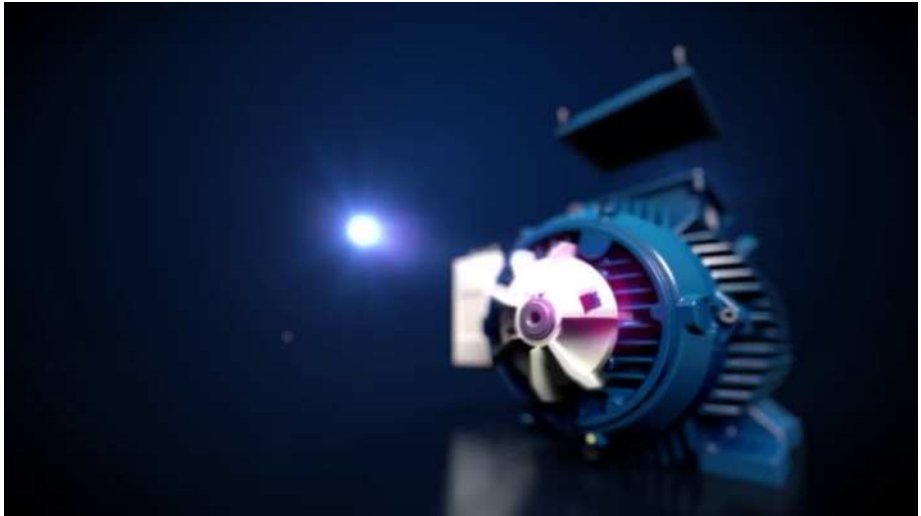
- (very) cheap
- high efficiency feasible (IE4)
- high power density and torque-per-volume ratio
- sensorless control feasible

disadvantages:

- power factor
- highly nonlinear
- inverter necessary
- (nonlinear control and good system knowledge necessary)

Motivation and problem formulation

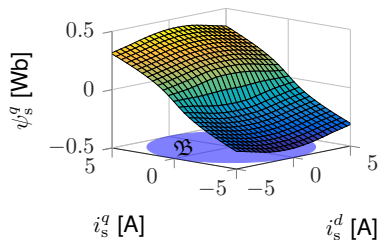
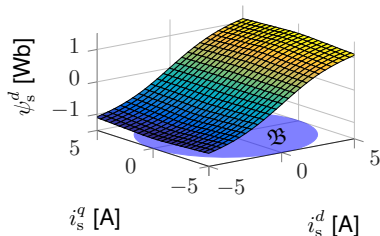
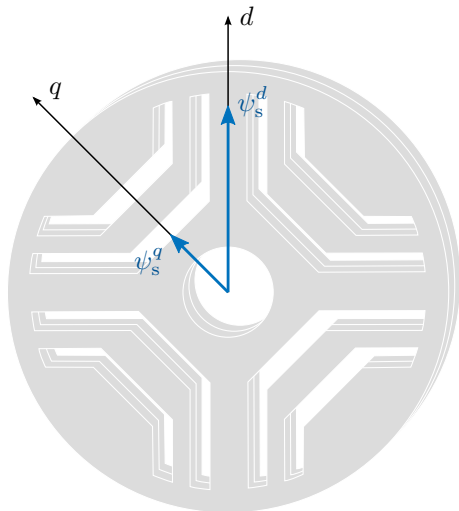
Reluctance synchronous machine: A look inside



http://www.youtube.com/watch?v=69mtuom774E&index=4&list=PLg4s1do3XuV1wc1Lnpy2gvfjd_o4wtA_D (cut version/duration: 0:26 min)

Motivation and problem formulation

Flux linkage in the RSM

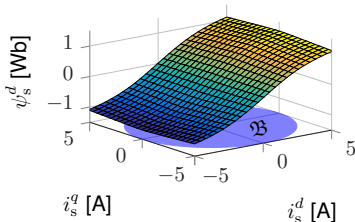


Motivation and problem formulation

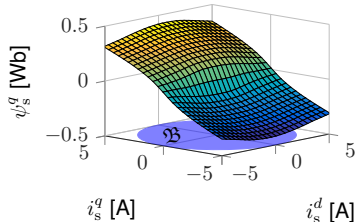
Control objective: Current reference tracking with prescribed transient accuracy

$$\mathbf{u}_s^k(t) = R_s \mathbf{i}_s^k(t) + \frac{d}{dt} \psi_s^k(\mathbf{i}_s^k(t)) + \omega_k(t) \underbrace{\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}}_{=: \mathbf{J}} \psi_s^k(\mathbf{i}_s^k(t)), \quad (1)$$

$$\frac{d}{dt} \omega_k(t) = \frac{p}{\Theta} \left[\underbrace{\frac{3}{2} p \mathbf{i}_s^k(t)^\top \mathbf{J} \psi_s^k(\mathbf{i}_s^k(t))}_{\text{machine torque}} - \underbrace{m_l(t)}_{\text{loads}} - \underbrace{(\nu \omega_k(t) + (\mathfrak{F} \omega_k)(t))}_{\text{friction}} \right], \quad (2)$$



d-flux linkage



q-flux linkage

Outline

2 Current PI-funnel control with anti-windup for RSMs [1]

- Motivation and problem formulation
- **Structural system properties of the RSM**
- PI-funnel control with anti-windup
- Implementation and results

Structural system properties of the RSM

Derivation of the nonlinear current dynamics

- To be derived: Nonlinear current dynamics

$$\frac{d}{dt} \mathbf{i}_s^k(t) = \dots \quad (3)$$

- Given: Stator voltage equation

$$\mathbf{u}_s^k(t) = R_s \mathbf{i}_s^k(t) + \frac{d}{dt} \boldsymbol{\psi}_s^k(\mathbf{i}_s^k(t)) + \omega_k(t) \mathbf{J} \boldsymbol{\psi}_s^k(\mathbf{i}_s^k(t)), \quad \boldsymbol{\psi}_s^k(\mathbf{i}_s^k(0)) = \boldsymbol{\psi}_{s,0}^k$$

Assumption 1

Flux linkage $\boldsymbol{\psi}_s^k [\text{Wb}]^2$ is a continuously differentiable function of the stator currents $\mathbf{i}_s^k [\text{A}]^2$, i.e.

$$\boldsymbol{\psi}_s^k : \mathbb{R}^2 \rightarrow \mathbb{R}^2, \quad \mathbf{i}_s^k \mapsto \boldsymbol{\psi}_s^k(\mathbf{i}_s^k) \quad \wedge \quad \boldsymbol{\psi}_s^k(\cdot) \in \mathcal{C}^1(\mathbb{R}^2; \mathbb{R}^2) \quad (4)$$

Structural system properties of the RSM

Inductance matrix

Definition 1

Inductance matrix $\mathbf{L}_s^k [\text{H}]^{2 \times 2}$ is defined by

$$\mathbf{L}_s^k(\mathbf{i}_s^k) := \begin{bmatrix} L_s^{dd}(\mathbf{i}_s^k) & L_s^{dq}(\mathbf{i}_s^k) \\ L_s^{qd}(\mathbf{i}_s^k) & L_s^{qq}(\mathbf{i}_s^k) \end{bmatrix} := \left[\begin{array}{cc} \frac{\partial \psi_s^d(\mathbf{i}_s^k)}{\partial i_s^d} & \frac{\partial \psi_s^d(\mathbf{i}_s^k)}{\partial i_s^q} \\ \frac{\partial \psi_s^q(\mathbf{i}_s^k)}{\partial i_s^d} & \frac{\partial \psi_s^q(\mathbf{i}_s^k)}{\partial i_s^q} \end{array} \right] \bigg|_{\mathbf{i}_s^k} = \frac{\partial \psi_s^k(\mathbf{i}_s^k)}{\partial \mathbf{i}_s^k} \bigg|_{\mathbf{i}_s^k} \quad (5)$$

- symmetric [37]:

$$\forall \mathbf{i}_s^k \in \mathbb{R}^2: \mathbf{L}_s^k(\mathbf{i}_s^k) = \mathbf{L}_s^k(\mathbf{i}_s^k)^\top \Leftrightarrow L_s^{dq}(\mathbf{i}_s^k) = L_s^{qd}(\mathbf{i}_s^k) \quad (6)$$

- positive definite [37]:

$$\forall \mathbf{i}_s^k \in \mathbb{R}^2: \mathbf{L}_s^k(\mathbf{i}_s^k) > 0 \Leftrightarrow L_s^{dd}(\mathbf{i}_s^k) > 0, L_s^{qq}(\mathbf{i}_s^k) > 0, \det(\mathbf{L}_s^k(\mathbf{i}_s^k)) > 0 \quad (7)$$

Structural system properties of the RSM

Generic model with nonlinear current dynamics

Time derivatives of the flux linkage are given by:

$$\frac{d}{dt} \psi_s^k(i_s^k(t)) = \frac{\partial \psi_s^k(i_s^k(t))}{\partial i_s^k(t)} \frac{d}{dt} i_s^k(t) \stackrel{(5)}{=} \mathbf{L}_s^k(i_s^k(t)) \frac{d}{dt} i_s^k(t) \quad (8)$$

Inserting (8) into (1) yields **nonlinear current dynamics**:

$$\left[\begin{array}{l} \frac{d}{dt} i_s^k(t) = \mathbf{L}_s^k(i_s^k(t))^{-1} \left[\text{sat}_{\hat{u}}(\mathbf{u}_s^k(t)) - R_s i_s^k(t) - \omega_k(t) \mathbf{J} \psi_s^k(i_s^k(t)) \right] \\ \frac{d}{dt} \omega_k(t) = \frac{p}{\Theta} \left[\underbrace{\frac{3}{2} p i_s^k(t)^\top \mathbf{J} \psi_s^k(i_s^k(t))}_{\text{machine torque}} - \underbrace{m_l(t)}_{\text{loads}} - \underbrace{(\nu \omega_k(t) + (\mathfrak{F} \omega_k)(t))}_{\text{friction}} \right] \end{array} \right] \quad (9)$$

with system properties (see Remark IV.1):

- 2-input 2-output system with vector relative degree **one**!
- BIBO stable internal dynamics, i.e. $i_s^k(\cdot) \in \mathcal{L}^\infty \wedge m_l(\cdot) \in \mathcal{L}^\infty \Rightarrow \omega_k(\cdot) \in \mathcal{L}^\infty$
- Euclidean input saturation [38], i.e. $\|\mathbf{u}_s^k(t)\| \leq \hat{u} := \frac{u_{dc}}{2}$ for all $t \geq 0$

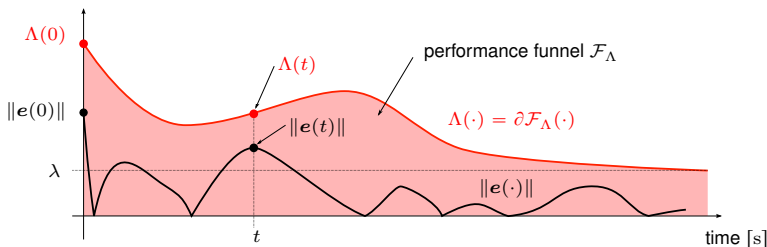
Outline

2 Current PI-funnel control with anti-windup for RSMs [1]

- Motivation and problem formulation
- Structural system properties of the RSM
- PI-funnel control with anti-windup
- Implementation and results

Current PI-funnel control with anti-windup for RSMs

Funnel control: Tracking with prescribed transient accuracy



Controller (applicable if feasibility condition $\hat{u} \geq \hat{u}_{\text{feas}}$ holds, see Theorem IV.2):

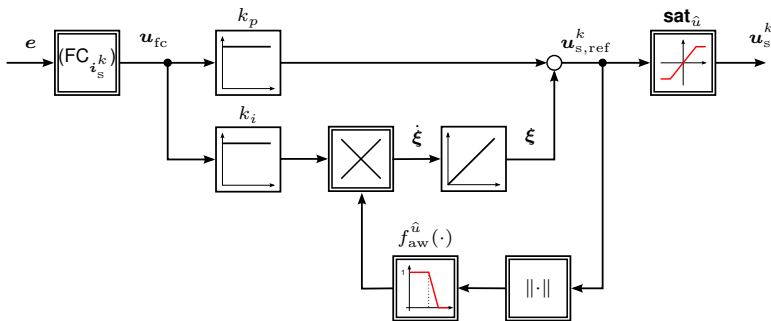
$$\boxed{\mathbf{u}_{\text{fc}}(t) = k(t)\mathbf{e}(t)} \quad \implies \quad \boxed{\|\mathbf{e}(t)\| < \Lambda(t)} \quad (\text{FC}_{\mathbf{i}_s^k})$$

where

- $\mathbf{e}(t) = (e_s^d(t), e_s^q(t))^T = \mathbf{i}_{s,\text{ref}}^k(t) - \mathbf{i}_s^k(t)$
- $k(t) = \frac{1}{\Lambda(t) - \|\mathbf{e}(t)\|} \geq \frac{1}{\Lambda(t)} \quad \text{and} \quad \|\mathbf{e}(t)\| = \sqrt{e_s^d(t)^2 + e_s^q(t)^2}$

Current PI-funnel control with anti-windup for RSMs

PI-funnel control with anti-windup



$$\left. \begin{aligned} \frac{d}{dt} \boldsymbol{\xi}(t) &= k_i f_{aw}^{\hat{u}} \left(\boldsymbol{\xi}(t) + k_p \mathbf{u}_{fc}(t) \right) \mathbf{u}_{fc}(t), & \boldsymbol{\xi}(0) &= \boldsymbol{\xi}^0 \in \mathbb{R}^n \\ \mathbf{u}_{s,ref}^k(t) &= \boldsymbol{\xi}(t) + k_p \mathbf{u}_{fc}(t), & \text{where } k_p > 0, k_i \geq 0. \end{aligned} \right\} \quad (\text{PI}^{aw})$$

⇒ $\boldsymbol{\xi}(\cdot)$ acts as bounded input disturbance (see Lemma III.1)

⇒ PI-like extension for steady state accuracy

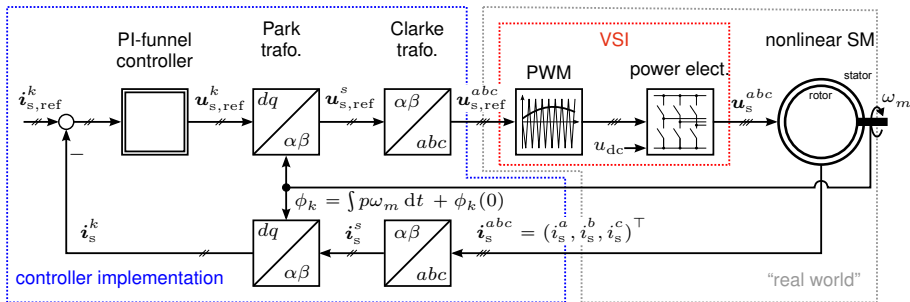
Outline

2 Current PI-funnel control with anti-windup for RSMs [1]

- Motivation and problem formulation
- Structural system properties of the RSM
- PI-funnel control with anti-windup
- Implementation and results

Current PI-funnel control with anti-windup for RSMs

Control-loop and implementation

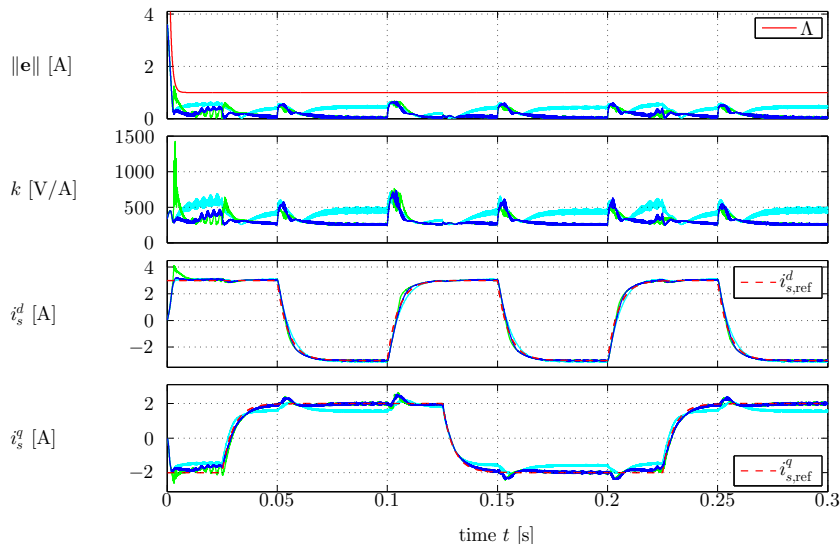


Realistic modeling:

- three-phase signals (machine, inverter, modulation, ...)
- pulse width modulation (PWM) and switching behavior of voltage source inverter (VSI)
- Park-/Clarke transformation

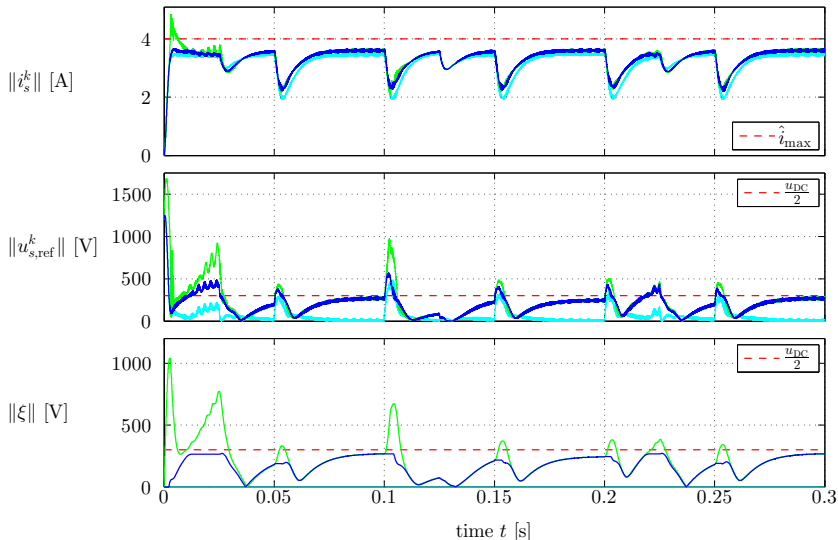
Current PI-funnel control with anti-windup for RSMs

Simulation results (1.1 kW RSM): — FC, — FC+PI and — FC+PI^{aw}



Current PI-funnel control with anti-windup for RSMs

Simulation results (1.1 kW RSM): — FC, — FC+PI and — FC+PI^{aw}



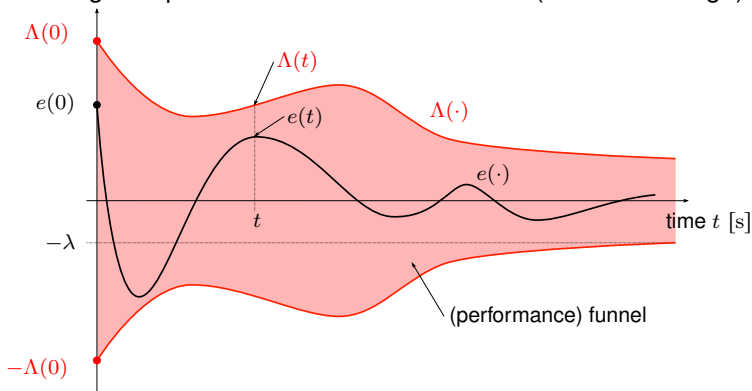
Outline

3 Conclusion

Conclusion

Funnel control: Facts

- **simple** and **robust** controller
- Tracking with prescribed **transient behavior** ($\rightarrow$ funnel design)



- **asymptotic accuracy** possible ($\rightarrow$ internal model design, e.g. PI)

— **Happy Birthday, Achim and thank you for all your time and support!** —

References I

- [1] Christoph M. Hackl. Current PI-funnel control with anti-windup for synchronous machines. In *Proceedings of the 54th IEEE Conference on Decision and Control*, pages 1997–2004, 2015.
- [2] Hans Schuster, Christian Westermaier, and Dierk Schröder. High-gain control of systems with arbitrary relative degree: Speed control for a two mass flexible servo system. In *Proceedings of the 8th IEEE International Conference on Intelligent Engineering Systems*, pages 486–491, Cluj-Napoca, Romania, 2004.
- [3] Hans Schuster, Christoph M. Hackl, Christian Westermaier, and Dierk Schröder. Funnel-control for electrical drives with uncertain parameters. In *Proceedings of the 7th International Power Engineering Conference*, Singapore, 2005.
- [4] Hans Schuster, Christian Westermaier, and Dierk Schröder. Non-identifier-based adaptive control for a mechatronic system achieving stability and steady state accuracy. In *Proceedings of the Joint CCA, ISIC and CACSD*, pages 1819–1824, Munich, Germany, 2006.
- [5] Hans Schuster, Christian Westermaier, and Dierk Schröder. Non-identifier-based adaptive speed control for a two-mass flexible servo system: Consideration of stability and steady state accuracy. In *Proceedings of the 14th Mediterranean Conference on Control and Automation*, pages 1–6, 2006.
- [6] Hans Schuster, Christian Westermaier, and Dierk Schröder. Non-identifier-based adaptive tracking control for a two-mass system. In *Proceedings of the International Conference on Intelligent Engineering Systems*, pages 190–195, 2006.
- [7] Christoph M. Hackl and Dierk Schröder. Funnel-control for nonlinear multi-mass flexible systems. In *Proceedings of the 32nd Annual Conference on IEEE Industrial Electronics*, pages 4707–4712, 2006.
- [8] Christoph M. Hackl, Hans Schuster, Christian Westermaier, and Dierk Schröder. Funnel-control with integrating prefilter for nonlinear, time-varying two-mass flexible servo systems. In *Proceedings of the 9th International Workshop on Advanced Motion Control*, pages 456–461, Istanbul, Turkey, 2006.

References II

- [9] Christoph M. Hackl, Yang Ji, and Dierk Schröder. Enhanced funnel-control with improved performance. In *Proceedings of the 15th Mediterranean Conference on Control and Automation*, pages Paper T01–016, 2007.
- [10] Christoph M. Hackl, Yang Ji, and Dierk Schröder. Funnel-control with constrained control input compensation. In *Proceedings of the 9th IASTED International Conference CONTROL AND APPLICATIONS*, pages 147–152, 2007.
- [11] Christoph M. Hackl and Dierk Schröder. Funnel-control with online foresight. In *Proceedings of the 26th IASTED International Conference MODELLING, IDENTIFICATION AND CONTROL*, pages 171–176, 2007.
- [12] Christoph M. Hackl, Yang Ji, and Dierk Schröder. Nonidentifier-based adaptive control with saturated control input compensation. In *Proceedings of the 15th Mediterranean Conference on Control and Automation*, pages Paper T01–15, 2007.
- [13] Christoph M. Hackl, Christian Endisch, and Dierk Schröder. Applicability of funnel-control in robotics. In *Proceedings of the 5th International Conference on Computational Intelligence, Robotics and Autonomous Systems*, pages 65–70, 2008.
- [14] Christoph M. Hackl, Christian Endisch, and Dierk Schröder. Error reference control of nonlinear two-mass flexible servo systems. In *Proceedings of the 16th Mediterranean Conference on Control and Automation*, pages 1047–1053, 2008.
- [15] Christoph M. Hackl, Christian Endisch, and Dierk Schröder. Funnel-control in robotics: An introduction. In *Proceedings of the 16th Mediterranean Conference on Control and Automation*, pages 913–919, 2008.
- [16] Christoph M. Hackl, Christian Endisch, and Dierk Schröder. Specially designed funnel-control in mechatronics. In *Proceedings of the 5th International Conference on Computational Intelligence, Robotics and Autonomous Systems*, pages 59–64, 2008.

References III

- [17] Christoph M. Hackl and Dierk Schröder. Non-identifier based adaptive control in robotics: An introduction. *International Journal of Factory Automation, Robotics and Soft Computing*, 4:90–99, 2008.
- [18] Christoph M. Hackl, Christian Endisch, and Dierk Schröder. Contributions to non-identifier based adaptive control in mechatronics. *Robotics and Autonomous Systems, Elsevier*, 57(10):996–1005, 2009.
- [19] Hans Schuster. *Hochverstärkungsbasierte Regelung nichtlinearer Antriebssysteme*. PhD thesis, Lehrstuhl für Elektrische Antriebssysteme, Technische Universität München (TUM), Germany, 2009.
- [20] Christoph M. Hackl and Dierk Schröder. Non-identifier based adaptive control in robotics: An introduction. In Salvatore Pennacchio, editor, *Recent advances in Control Systems, Robotics and Automation*, volume 1. INTERNATIONALSAR International Society for Advanced Research, Palermo, Italy, third edition, 2009.
- [21] Christoph M. Hackl. Funnel Control: Implementierung, Erweiterung und Anwendung. In Dierk Schröder, editor, *Intelligente Verfahren: Systemidentifikation und Regelung nichtlinearer Systeme*, pages 697–760. Springer-Verlag, Berlin, 2010.
- [22] Achim Ilchmann and Hans Schuster. PI-funnel control for two mass systems. *IEEE Transactions on Automatic Control*, 54(4):918–923, 2009.
- [23] Christoph M. Hackl, Andreas G. Hofmann, Rik W. De Doncker, and Ralph M. Kennel. Funnel control for speed & position control of electrical drives: A survey. In *Proceedings of the 19th Mediterranean Conference on Control and Automation*, pages 181–188, 2011.
- [24] Christoph M. Hackl, Andreas G. Hofmann, and Ralph M. Kennel. Funnel control in mechatronics: An overview. In *Proceedings of the 50th IEEE Conference on Decision and Control and European Control Conference*, pages 8000–8007, 2011.

References IV

- [25] Christoph M. Hackl. 'Funnel control' zur Positionsregelung von starren Drehgelenkrobotern mit grob bekannter Trägheitsmatrix. In *Tagungsband des GMA-Fachausschuss 1.40*, pages 302–310, 2012.
- [26] Christoph M. Hackl and Ralph M. Kennel. Position funnel control for rigid revolute joint robotic manipulators with known inertia matrix. In *Proceedings of the 20th Mediterranean Conference on Control and Automation*, pages 615–620, 2012.
- [27] Christoph M. Hackl and Ralph M. Kennel. Position funnel control with linear internal model. In *Proceedings of 2012 IEEE International Conference on Control Applications*, pages 1334–1339, 2012.
- [28] Christoph M. Hackl, Norman Hopfe, Achim Ilchmann, Markus Mueller, and Stephan Trenn. Funnel control for systems with relative degree two. *SIAM Journal on Control and Optimization*, 51(2):965–995, 2013.
- [29] Christoph M. Hackl. Funnel control with disturbance observer for two-mass systems. In *Proceedings of the 52nd IEEE Conference on Decision and Control*, pages 6244–6249, 2013.
- [30] Christoph M. Hackl. PI-funnel control with Anti-windup and its application for speed control of electrical drives. In *Proceedings of the 52nd IEEE Conference on Decision and Control*, pages 6250–6255, 2013.
- [31] Christoph M. Hackl. Funnel control for wind turbine systems. In *Proceedings of the 2014 IEEE International Conference on Control Applications*, pages 1377–1382, 2014.
- [32] Christoph M. Hackl. Speed funnel control with disturbance observer for wind turbine systems with elastic shaft. In *Proceedings of the 54th IEEE Conference on Decision and Control*, pages 2005–2012, 2015.
- [33] Christoph M. Hackl. *Non-identifier based adaptive control in mechatronics: Theory and Application*. Lecture Notes in Control and Information Sciences. Springer-Verlag, Berlin, 2015 (accepted; final version in preparation).

References V

- [34] Marten J. Kamper, F.S. van der Merwe, and S. Williamson. Direct finite element design optimisation of the cageless reluctance synchronous machine. *IEEE Transactions on Power Conversion*, 11(3):547–555, 1996.
- [35] Thomas A. Lipo. Synchronous reluctance machines – A viable alternative for AC drives? *Electric Machines & Power Systems*, 19(6):659–671, 1991.
- [36] A. Vagati. The synchronous reluctance solution: A new alternative in AC drives. In *Proceedings of the 20th International Conference on Industrial Electronics, Control and Instrumentation*, pages 1–13, 1994.
- [37] Michael T. Ivrlač. Lecture notes on Circuit Theory and Communications. Lecture notes (version 2.1), Institute for Circuit Theory and Signal Processing, Technische Universität München, 2013.
- [38] Norman Hopfe, Achim Ilchmann, and Eugene P. Ryan. Funnel control with saturation: Linear MIMO systems. *IEEE Transactions on Automatic Control*, 55(2):532–538, 2010.

Outline

4 Appendix

Structural system properties of the RSM

Nonlinear inductances $L_s^d := \frac{\partial \psi_s^d}{\partial i_s^d}$, $L_s^q := \frac{\partial \psi_s^q}{\partial i_s^q}$, $L_s^{dq} := \frac{\partial \psi_s^d}{\partial i_s^q} = \frac{\partial \psi_s^q}{\partial i_s^d} =: L_s^{qd}$

